



Supplementary Materials

Text S1. Study Area

The study site was an urban area located in Gwangju (35°09'33.12"N, 126°50'49.63"E), a southern province of South Korea. It covered an area of 0.0125 km² and included a separated sewer system. This urban area was originally planned and developed during the 1990s in South Korea. The study area was a commercial zone characterized by predominantly impermeable surfaces (~85%), including office buildings, a parking lot, and restaurants, along with a residential area. The climate of the study area is classified as monsoon, with heavy rainfall concentrated in the summer season. It shows an average annual rainfall of 1,391 mm, with maximum temperature of 29.3°C and minimum temperature of -1.9°C [Fig. S1].

Text S2. LID Modules in the SWMM

The calculation of infiltration fluxes in the surface layer involves considering both direct runoff and runoff from the impervious layer [1]. In this study, the infiltration rate (f_1) (cm min⁻¹) is estimated using the following Green-Ampt equation [2] [Fig. 2(a)]:

$$f_1 = K_s \left(1 + \frac{(\phi - \theta_1)(d_1 + \psi)}{F} \right) \quad (S1)$$

Here, K_s indicates the soil's saturated hydraulic conductivity (cm min⁻¹), θ_1 denotes the moisture content at the top of the soil layer, d_1 indicates the pond depth on the surface (cm), ψ indicates the suction head where infiltration wetting occurs, and F represents the cumulative total amount of water infiltrated per unit area. The modified Green-Ampt equation provides an estimation of the infiltration rate, corresponding to the intensity of rainfall until the soil reaches saturation [3].

The soil layer simulates the movement of water (f_2) from the soil into the storage layer [Fig. 2(b)]. The movement of water in soil can be calculated using the following Darcy's law, which employs the same approach as the SWMM groundwater module [1].

$$f_2 = K_s \exp(-HCO(\phi - \theta_2)), \theta_2 > \theta_{FC} \quad (S2)$$

$$f_2 = 0, \theta_2 \leq \theta_{FC} \quad (S3)$$

Here, f_2 denotes the rate of soil percolation (cm min⁻¹), the decay constant HCO is obtained from the moisture retention curve, θ_2 represents the moisture content of the soil layer, and θ_{FC} refers to the moisture content at field capacity in the soil.

Text S3. HYDRUS-1D

The governing equation for the flow of variably saturated soil can be calculated using the Richards equation [4]:

$$\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial z} \left[K(h) \left(\frac{\partial h}{\partial z} + 1 \right) \right] \quad (S4)$$

Here, θ represents the volumetric soil water content (L L⁻¹), t denotes the time (T⁻¹), $K(h)$ indicates the hydraulic conductivity (LT⁻¹), h represents the soil water pressure head (L), and Z represents the vertical space (L).

The van Genuchten model for hydraulic properties is represented by the following equations [4, 5]:

$$\frac{\theta - \theta_r}{\phi - \theta_r} = \left[\frac{1}{1 + (a\psi)^n} \right]^m \quad (S5)$$

$$\frac{K(h)}{K_{sat}} = \left(\frac{\theta - \theta_r}{\phi - \theta_r} \right)^{1/2} \left[1 - \left(1 - \left(\frac{\theta - \theta_r}{\phi - \theta_r} \right)^{\frac{1}{m}} \right)^m \right]^2 \quad (S6)$$

where θ is the water content (L L⁻¹), θ_r is the residual water content (L L⁻¹), ϕ is the porosity (L L⁻¹), $m = 1 - 1/n$, $K(h)$ represents the hydraulic conductivity (LT⁻¹), and K_{sat} is the saturated hydraulic conductivity (LT⁻¹).

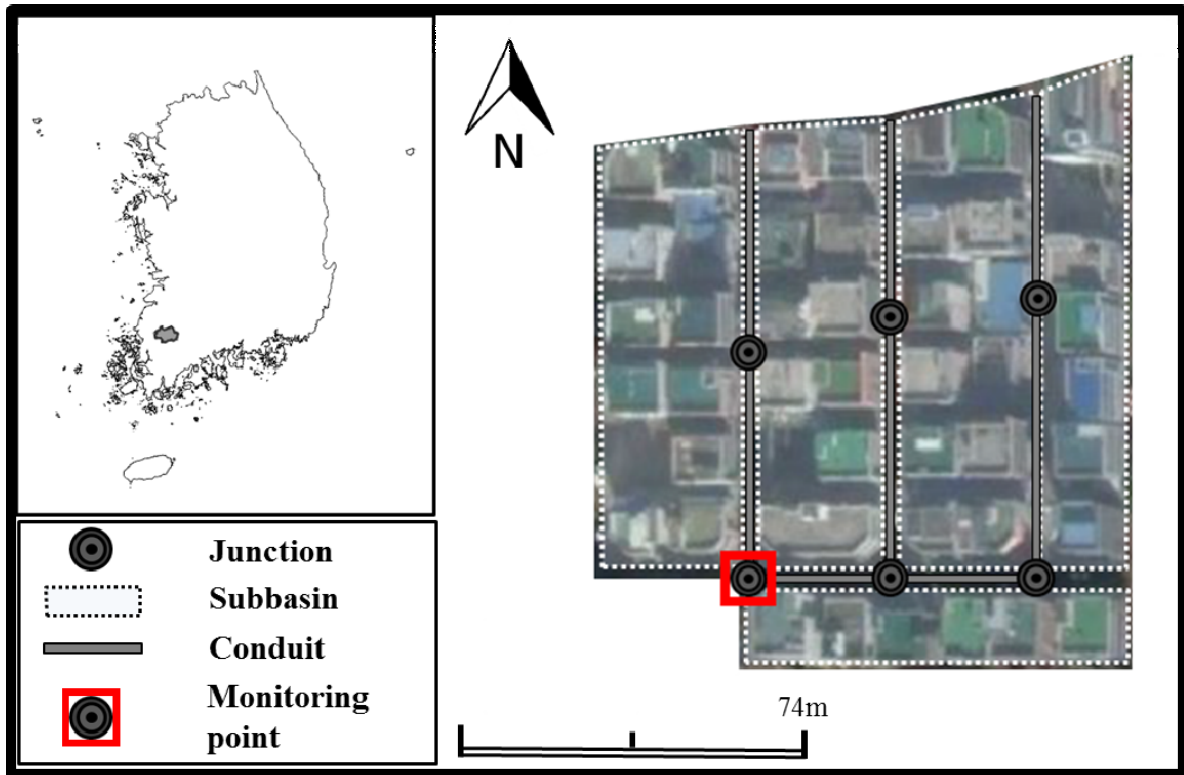


Fig. S1. Map of the study area, including junctions, sub-basins, conduits, and the monitoring location (35°09'33.12"N, 126°50'49.63"E) (Google, 2014).

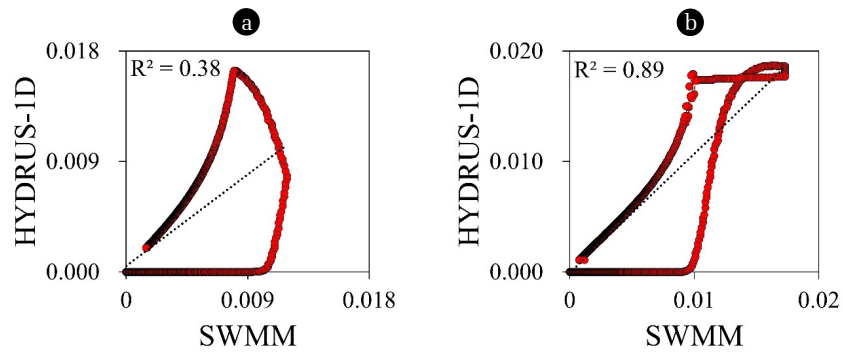


Fig. S2. Scatter plots of infiltration rates between the SWMM and the HYDRUS-1D model's under (a) unsaturated soil and (b) saturated soil conditions.

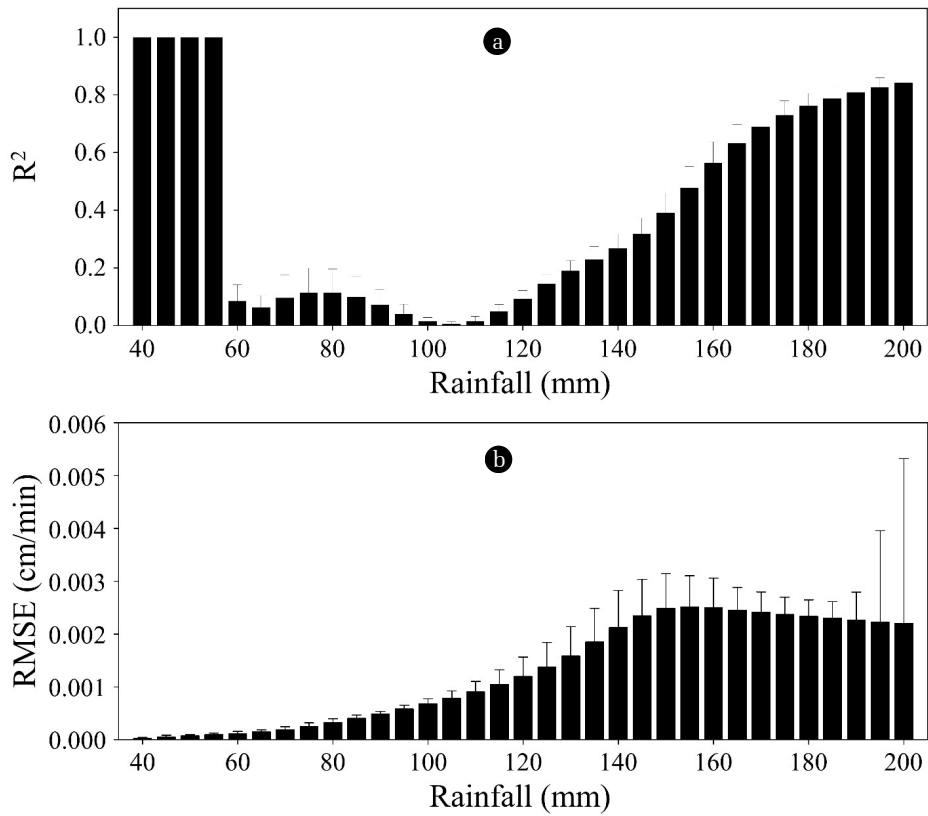


Fig. S3. (a) R^2 and (b) RMSE values of the SWMM evaluated with the HYDRUS-1D model's infiltration rate under different rainfall scenarios.

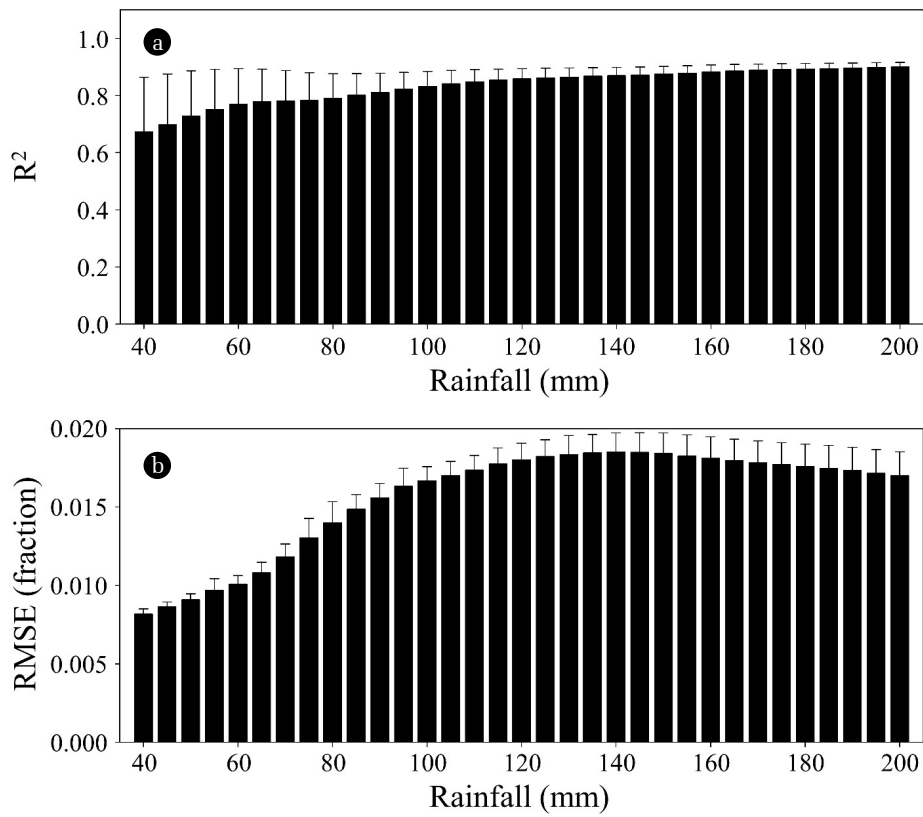


Fig. S4. (a) R^2 and (b) RMSE values of the SWMM evaluated with the HYDRUS-1D model's soil moisture under different rainfall scenarios.

Table S1. Sensitivity of infiltration-related parameters in the SWMM with different ranges of rainfall volume (mean \pm SD).

Parameters	Rainfall volume (mm)			
	0~50	50~100	100~150	150~200
<i>Mean of EEs</i>				
Field capacity	233 \pm 182	243 \pm 189	247 \pm 188	223 \pm 164
Porosity	35.4 \pm 20.6	40.6 \pm 34.4	36.9 \pm 21.7	37.1 \pm 23.9
Saturated K	21.3 \pm 13.1	22.0 \pm 14.1	24.1 \pm 16.0	23.4 \pm 15.0
K-slope	20.2 \pm 10.3	20.9 \pm 10.3	19.9 \pm 9.2	20.5 \pm 10.6
Suction head	0.029 \pm 0.033	0.032 \pm 0.036	0.038 \pm 0.061	0.078 \pm 0.232
<i>Standard deviation of EEs</i>				
Field capacity	297 \pm 284	357 \pm 421	329 \pm 256	278 \pm 220
Porosity	55.9 \pm 32.7	80.9 \pm 145.0	56.7 \pm 35.3	64.4 \pm 51.3
Saturated K	41.3 \pm 23.9	44.2 \pm 30.0	53.3 \pm 45.8	48.6 \pm 33.6
K-slope	32.6 \pm 12.2	33.5 \pm 12.1	32.6 \pm 11.6	32.8 \pm 12.5
Suction head	0.095 \pm 0.101	0.120 \pm 0.127	0.146 \pm 0.227	0.448 \pm 1.55

Table S2. Sensitivity of underdrain-related parameters in the SWMM with different ranges of rainfall volume (mean \pm SD).

Parameters	Rainfall volume (mm)			
	0~50	50~100	100~150	150~200
<i>Mean of EEs</i>				
Flow Coefficient	0.31 \pm 0.33	2.93 \pm 0.57	3.29 \pm 0.43	3.57 \pm 0.60
Flow Exponent	2.89 \pm 2.94	12.1 \pm 0.52	12.7 \pm 0.43	13.0 \pm 0.31
<i>Standard deviation of EEs</i>				
Flow Coefficient	0.62 \pm 0.69	4.14 \pm 2.72	4.01 \pm 1.78	5.04 \pm 2.95
Flow Exponent	2.36 \pm 2.45	3.40 \pm 0.53	3.82 \pm 0.60	3.88 \pm 0.54

References

1. Rossman LA, Huber WC. Storm Water Management Model Reference Manual, Volume III – Water Quality, EPA/600/R-16/093. U.S. Environmental Protection Agency, Cincinnati, OH 2016.
2. Mein RG, Larson CL. Modeling infiltration during a steady rain. *Water Resour. Res.* 1973;9(2):384-394. doi.org/10.1029/WR009i002p00384
3. Almedej J, Esen II. Modified Green-Ampt infiltration model for steady rainfall. *J. Hydrol. Eng.* 2014;19(9): 04014011. doi.org/10.1061/(ASCE)HE.1943-5584.000094
4. Šimůnek J, van Genuchten MT, Šejna M. The HYDRUS-1D Software Package For Simulating The One-Dimensional Movement of Water, Heat and Multiple Solutes in Variably-saturated Media, Version 3.0. Department of Environmental Sciences, University of California Riverside, Riverside, California, USA; 2005.
5. van Genuchten MT. A closed-form equation for predicting the hydraulic conductivity of unsaturated soils. *Soil Sci. Soc. Am. J.* 1980;44(5):892-898. doi.org/10.2136/sssaj1980.03615995004400050002x