Adsorption of crystal violet dye by agricultural rice bran waste: Isotherms, kinetics, modeling and influencing factors

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ABSTRACT
In this study, the potential of modified rice bran (MRB) was investigated for the elimination of crystal violet (CV) from plotted effluent. In this regard, rice bran (RB) was modified by chlorosulfonic acid. The results of FTIR, EDX, and SEM analysis showed structural change, an increase in the amount of sulfur, and the formation of a new band (998 and 1,225 cm$^{-1}$) in MRB, respectively. The impact of different variables such as contact time, MRB dosage, pH, CV concentration, and ions content on removal efficiency was studied by using batch experiments. In addition, response surface methodology was employed to optimize the experiments. The maximum removal efficiency of 97.4% was obtained at the adsorbent dosage of 2 g L$^{-1}$, initial CV concentration of 100 mg L$^{-1}$, and contact time of 42.75 min. The highest adsorption capacity of 603 mg g$^{-1}$ was acquired by the Langmuir model. The best description of kinetic data was achieved by the Elovich model. The thermodynamic study of the adsorption indicated an endothermic and spontaneous reaction. MRB could be regenerated by HCl 0.5 mol L$^{-1}$ and removal efficiency was declined 10 percent after 5 adsorption/desorption cycles. It was concluded that MRB is an operational adsorbent to remove CV from effluents.

Keywords: Crystal violet, Kinetics, Low-cost adsorbent, Rice bran, Response Surface Methodology

1. Introduction

The emission of dyes by various industries into water bodies is a serious hazard for humans and the environment due to different chemical compounds and toxic materials [1, 2]. Globally, each year, 0.7 billion tons of paints are produced [3]. One of the popular pigments in the dyeing of cotton, silk, and wool is Crystal violet (CV). Aquaculture industries use this material as fungicide and antiseptic agents, and laboratories use it as an indicator because of its low cost and capabilities [4]. CV have cytogenetic effects on cells [5–7]. It can cause sore eyes, light sensitivity, digestive system irritability, and toxicity for mammals’ cells [8, 9]. It has been reported that in high concentrations, it causes respiratory and kidney failure, cancer, and permanent blindness [10]. Moreover, another study also showed that CV even at low concentrations can cause induced cell death [11]. Considering extensive uses of crystal violet in industries despite its hazards, its removal from aqueous solutions is vital.

Different techniques have been evolved for the treatment of dyeing industries effluents in recent years, including adsorption [12], ultrafiltration [13], ozonation [14], precipitation [15], reverse osmosis [16], electrocoagulation [17], microbial degradation [18] and oxidative degradations [19]. Nevertheless, almost all mentioned techniques suffer from various disadvantages, such as inefficiency, temperature and pH sensitivity, secondary pollutions, high cost, and small scale application [20, 21]. Among these methods, the adsorption method is known to be an efficient process for the treatment of dyed effluents due to its high efficiency, accessibility, flexibility, insensitivity to toxic materials, and its ease of work and administration compared to other conventional methods [22]. But, choosing adsorbent materials can escalate the cost. The by-products or wastes of agricultural activities such as banana peels [23], walnut wood [24], orange peels [25], sugarcane bagasse [26], rice husk [27], peanut hull [28, 29], Mango stone [30], Musa paradisiaca peels [31] and sweet potato peels [32] have been studied by researchers. However, adsorbents with high efficiency, availability, and low price are still needed.

Rice bran, which considered as food waste is a byproduct of the rice milling industry [33]. It mainly consists of cellulose, hemicellulose, lignin, and protein [34]. These materials, due to having molecules with active sites such as hydroxyl, carboxyl, and amino groups can easily attach to dyes [4]. They are also highly stable
both chemically and physically [33]. Producing an adsorbent from cellulosic waste for treatment of dyes in effluent which have economic and environmental benefits, seems a proper replacement for conventional disposal methods.

The aim of the present study is to provide an effective adsorbent by chemical modification of rice bran, and finally its effectiveness in removing CV from polluted effluents was studied. Modified rice bran (MRB) and rice bran were characterized by Fourier transform infrared (FTIR), energy-dispersive X-ray spectroscopy (EDX), and scanning electron microscopy (SEM). To optimize the influential parameters (contact time, initial concentration, and adsorbent dosage) on the response of CV removal, response surface methodology (RSM) was used. Also, kinetics, equilibrium isotherms, different ions, and thermodynamics of adsorption were used to assess the results. Finally, the adsorbent regeneration was investigated.

2. Material and Methods

2.1. Materials

CV with a color index 42555, λ\text{max} of 590 nm, and chemical formula C_{25}H_{30}N_{3}Cl was purchased from Sigma–Aldrich. To prepare the stock solution of CV (1,000 mg L^{-1}), 250 ml of distilled water was used to dissolve 273.8 mg of CV. In all experiments, Deionized water was applied. Also, chlorosulfonic acid (CSA, HSO_{3}Cl, 97% wt), dimethylformamide (DMF, C_{3}H_{7}NO, 99% wt), HCl, and NaOH was used. Also, the rice bran, which is a side product of the rice milling industry, was gathered from a grinding mill.

2.2. Adsorbent Preparation

In order to dry the rice bran, it was placed in an oven at 50 °C for 24 h. Then by sieving the dried barn, particles smaller than 425 μm were separated. In a typical procedure, 8 g of the extracted bran was mixed with 100 ml of DMF for 15 min. 20 g of CSA has been steadily mixed with 100 ml of DMF cautiously, then the mixed solution was placed in an ice bath. Subsequently, the resulting mixture was applied to RB and DMF gently and was shaken for 2 h at ambient temperature. The mixture was filtered using a 1μm membrane and neutralized by the proper amount of a sodium bicarbonate solution. The resulting mixture was washed several times by distilled water and filtered again. Finally, the mixture was dried at ambient temperature to obtain MRB. The corresponding process is shown in Fig. S1 (a), (b). The large volume of resulting DMF can be recycled at the end of reactions.

2.3. Characterization of MRB

For observation of active available functional groups of the adsorbent, the Fourier transform infrared (Bruker FTIR) analysis was used. Using scanning electron microscopy (SEM, model: HITACHI S-4160) the dimensions and morphology of the rice bran and MRB were studied. The composition of these materials was characterized by energy-dispersive X-ray spectroscopy (EDAX) and field emission scanning electron microscopy (FESEM, model: Mira 3-XMU).

2.4. Batch Experiments Studies

The removal of CV by MRB was carried out in a batch system. For this purpose, 50 mL of CV solution was mixed with an adequate amount of the adsorbent (0.01 – 0.1 g). Then it was agitated with a shaker at 150 rpm at a fixed temperature. The initial pH (2–10) was adjusted using diluted HCl and NaOH solutions. Isotherms with various CV concentration (100 – 1,000 mg L^{-1}) was studied while other parameters were kept constant. The kinetic study was carried out by altering the contact time from 2 to 60 min. Additionally, the temperature varied between 279 and 328 K to analyze thermodynamic parameters.

Afterward, the residual CV was determined by a UV/Vis spectrophotometer (USA, DR 5000) at a peak wavelength of 590 nm. The removal percentage of CV by MRB was determined using the Eq. (1):

$$\% \text{Removal} = \left( \frac{C_0 - C_e}{C_0} \right) \times 100$$

In this equation, $C_0$ represents the final and $C_0$ shows the primary concentrations of CV [35].

2.5. Experimental Design and Optimization

The application of RSM is very common in the process of adsorption experiments planning for dye removal [9, 36]. The aim of using RSM is to concurrently optimize influential parameters in the adsorption process to find the best efficiency. The most important advantage of this methodology is reducing the number of experiments and preserving materials, energy, and time [37, 38]. RSM consists of statistical and mathematical techniques, which leads to a comprehensive analysis of the correlation between effective factors [25]. The Box-Behnken Design (BBD) is one of the significant designs of RSM. In this study, the BBD was used as a scheme in designing experiments for studying the correlation between the variables and predicting the most efficient conditions for the CV adsorption process, using the Design-Expert software (version, 10.0.4). Time (A: 2-60 min), initial concentrations of CV (C, 100–1,000 mg L^{-1}), and adsorbent dosage (B: 0.2–2 g L^{-1}) were selected as independent variables for the predicted response (Y), and it was also considered as dependent outputs. According to BBD, a set of 17 runs was administered, involving five centered points with three parameters at three levels, and the results were presented in Table S1.

The correlation of the independent parameters and predicted response is explained using the quadratic equation (2):

$$Y = b_0 + \sum_{i=1} b_i x_i + \sum_{i=1} b_i x_i^2 + \sum_{i<j} b_{ij} x_i x_j$$

Where $x_i$ and $x_j$ indicates are the independent variables as coded levels, $Y$ is the response, $b_0$, $b_i$, $b_i$, and $b_{ij}$ are the interaction, quadratic, linear, and intercept coefficients, respectively, and $n$ is the number of independent variables [38]. The reliability of the fitted model and the statistical significance were evaluated by the correlation coefficient $R^2$, analysis of variance (ANOVA), and P-value.

The compatibility of kinetic and equilibrium study with the experiment results was evaluated using the chi-square test ($\chi^2$)
and the residual root-mean-square error (RMSE). RMSE and $\chi^2$ must be minimum, and the best model is described by the minimum value for the error function \[39\].

### 3. Results and Discussion

#### 3.1. MRB Characterization

The microstructure of rice bran and MRB was pictured using SEM analysis (Fig. 1 (a)-(d)). Raw rice bran contains organic matters such as starch, protein, and hemicellulose, which dissolves in acidic medium and move to the surface of rice bran. White spots in Fig. 1 (c) are white agglomerates, which are removed by chemical modification of rice bran \[40\]. These modifications are the result of sulfonation and hydrolysis in the acidic environment. In addition to these results, Fig. S2 (a), (b) shows the energy dispersive spectrum (EDX). The amount of sulfur in raw rice bran increased from 0.19 to 3.02%, which indicates a successful chemical modification using chlorosulfonic acid.

Fig. 2 represents the FT-IR spectrum of rice bran and MRB. It is clear that the FT-IR spectrum of MRB shows an additional adsorption band at 998 and 1,225 cm$^{-1}$. These new bands are related to the S-O bond, which confirms that rice bran modification using chlorosulfonic acid was successful \[41\]. Adsorption band in the range of approximately 2,800-3,300 cm$^{-1}$ can be assigned to hydroxyl groups, which is related to its organic matters such as hemicellulose, protein, and lignin. \[42, 43\]. The peak at 2,921 cm$^{-1}$, which belongs to MRB, is almost vanished, demonstrating organic matters of raw rice bran were eliminated by CSA in the process of adsorbent synthesis.

Fig. 1. The SEM pictures of rice bran. ((a): × 5 KX; (c): × 50 KX and MRB (b): × 5 KX; (d): × 50 KX).

#### 3.2. Analysis of Variance (ANOVA)

The following quadratic model BBD was obtained using the analysis of variance. This model describes the removal efficiency ($Y$) as a function of the concentration of CV (CV), adsorbent dosage (Ads), and contact time (T).

\[ Y = 45.9295 + 1.4073 \times T + 55.7759 \times \text{Ads} - 0.09609 \times (3) \]
\[ CV + 0.14065 \times T \times \text{Ads} + 0.0004763 \times T \times CV + 0.02209 \times \text{Ads} \times CV - 0.0236 \times T^2 - 15.6112 \times \text{Ads}^2 \]

ANOVA results for the investigation of the model's validity and importance of variables are presented in Table 1. The large F-values and P-value of less than 0.05 show the significance of models and variables \[43\]. It is clear that linear terms of A (contact time), B (adsorbent dosage), and C (concentration of CV) and quadratic terms of A and B were considerable for CV removal using MRB. The interaction between variables (AC and BC) was notable. Furthermore, the F-value of the model which is 492.88 along with low high F-value and P-value \[p < 0.0001\] indicates the high validity of the model. Consistency of the adjusted $R^2$ and the anticipated $R^2$ values supports the model's precision \[44\]. Fig. 3 (a) represents the normal probability of residuals for the removal efficiency of CV by MRB. It shows the symmetrical arrangement of experimental data within the level of confidence for the quadratic model \[45\].

Fig. 3 (b)-(d) show the surface plots of the model, which helps to understand interactions between parameters. The impact of contact time and adsorbent dosage on the percentage of CV removal is presented in Fig. 3 (b). By increasing contact time and adsorbent dosage, the CV removal increased. The strong relation between adsorbent dosage and initial concentration of CV is seen in Fig. 3 (c). This relation can be deduced from low high F-value and P-value \[45\]. Increasing the adsorbent dosage increases the CV removal, this is a result of the increasing number of adsorbent active removing more dye from the aqueous solution \[46\]. Fig. 3 (d) shows the impact of contact time and initial concentration of pollutants. At low CV concentration, the adsorption process is faster because in this condition adsorbent active sites are more accessible to adsorbate molecules of dye \[47\]. Finally, the maximum removal efficiency of 97.4% was calculated by the model analysis at initial CV concentration of 100 mg L$^{-1}$, contact time of 42.75 min, and adsorbent dosage of 2 g L$^{-1}$. 

![Fig. 2. The plots of FTIR (a) Rice bran, (b) MRB.](image-url)
Table 1. ANOVA Result for CV Removal by MRB

<table>
<thead>
<tr>
<th>Term</th>
<th>Mean Square</th>
<th>Degree of Freedom</th>
<th>Sum of Square</th>
<th>F-value</th>
<th>p-value</th>
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<td>Model</td>
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<td>8</td>
<td>15418.15</td>
<td>161.23</td>
<td>&lt; 0.0001</td>
</tr>
<tr>
<td>A- contact time</td>
<td>869.43</td>
<td>1</td>
<td>869.43</td>
<td>72.73</td>
<td>&lt; 0.0001</td>
</tr>
<tr>
<td>B- Adsorbent</td>
<td>6683.5</td>
<td>1</td>
<td>6683.5</td>
<td>559.12</td>
<td>&lt; 0.0001</td>
</tr>
<tr>
<td>C- CV</td>
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<td>1</td>
<td>3773.16</td>
<td>315.65</td>
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<tr>
<td>AB</td>
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<td>53.9</td>
<td>4.51</td>
<td>0.0714</td>
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<tr>
<td>AC</td>
<td>154.54</td>
<td>1</td>
<td>154.54</td>
<td>12.93</td>
<td>0.0088</td>
</tr>
<tr>
<td>BC</td>
<td>178.76</td>
<td>1</td>
<td>178.76</td>
<td>14.95</td>
<td>0.0062</td>
</tr>
<tr>
<td>A²</td>
<td>1403.15</td>
<td>1</td>
<td>1403.15</td>
<td>117.38</td>
<td>&lt; 0.0001</td>
</tr>
<tr>
<td>B²</td>
<td>548.22</td>
<td>1</td>
<td>548.22</td>
<td>45.86</td>
<td>0.0003</td>
</tr>
<tr>
<td>Residual</td>
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<td>7</td>
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<tr>
<td>Lack of Fit</td>
<td>14.47</td>
<td>3</td>
<td>43.42</td>
<td>1.44</td>
<td>0.3564</td>
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<tr>
<td>Pure Error</td>
<td>10.06</td>
<td>4</td>
<td>40.25</td>
<td></td>
<td></td>
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<tr>
<td>Cor. Total</td>
<td>15</td>
<td>15</td>
<td>15501.82</td>
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Pred R² = 0.9599, R² = 0.9946, Adj. R² = 0.9884

Fig. 3. (a) Plot of normal probability for CV removal using MRB. 3D surface: (b) Time-MRB (c) MRB dosage-CV concentration (d) Time-CV concentration.
3.3. pH Effect on The Removal Efficiency

One of the most crucial parameters in dye removal is pH because it can affect the density of the adsorbent surface charge, thereby affecting the dye removal efficiency [43]. pH was investigated in range of 2 to 10 to study its impact on the CV removal by MRB. Fig. 4 (a) shows the results. Moreover, the point of zero charge for MRB was found at around 2. There is not a competition between H' ions and CV to occupy the active sites of MRB because sulfate group of MRB keeps its charge even in acidic medium. As a consequence, the removal efficiency was constant in pH range of 2-7. The pH\textsubscript{PZC} value confirmed these explanations. When pH goes up from 7 to 10, the removal efficiency increased because of precipitation of OH'.

3.4. Ions Effect

Impact of K\textsuperscript{+}, NO\textsubscript{3}\textsuperscript{-}, Na\textsuperscript{+}, SO\textsubscript{4}\textsuperscript{2-}, Ca\textsuperscript{2+}, Mg\textsuperscript{2+}, HCO\textsubscript{3}\textsuperscript{-} and Cl\textsuperscript{-} on CV removal by MRB was studied (Fig. 4 (b)). To compare the impact of different ions on the CV removal process, eight samples and a control sample were used. The control sample marked as A in the chart. Ca\textsuperscript{2+} and Mg\textsuperscript{2+} ions compete with CV for active adsorption sites because of their positive charges; therefore, thereby decreasing the removal efficiency. Na\textsuperscript{+} and K\textsuperscript{+} also present positive charge as Calcium and Magnesium. In Fig. 4, we can observe a small reduction in dy removal in the presence of Na\textsuperscript{+} and K\textsuperscript{+} ions. However, for Ca\textsuperscript{2+} and Mg\textsuperscript{2+}, this reduction was more evident, because these ions are divalent, while Na\textsuperscript{+} and K\textsuperscript{+} are monovalent, showing low interaction with positive active sites. The other ions did not affect the dye removal.

3.5. Equilibrium Studies

Different isotherm equations including Radke-Prausnitz, Freundlich, UT, Temkin, Langmuir, Redlich-Peterson, and, Dubinin-Radushkevich models were used to investigate the isotherms data in the equilibrium state [48–50]. Also, the linear form of these models was used and the results are represented in Table 2 for the adsorption of CV by MRB. Different error functions, represented in Table S2, are used to investigate the performance of these models. Redlich-Peterson, UT, and Radke-Prausnitz isotherms have the lowest errors, while maximum error belongs to Dubinin-Radushkevich model, which could not fit the data well. The fitting degree followed the sequence:

Radke-Prausnitz = UT = Redlich-Peterson > Langmuir > Temkin > Freundlich > Dubinin-Radushkevich.

The adsorption isotherms and experimental data are indicated in Fig. 5 (a). Also Residual graph for different isotherms are shown in Fig. 5 (b) which confirm the results of error analysis. Value of non-dimensional factor (R\textsubscript{L}) in the Langmuir model, for different initial concentration of CV, was calculated in the range of 0.11 to 0.5, suggesting a favorable process for adsorption of CV by MRB. It is known that a nearly zero value for 1/n\textsubscript{f} calculated by the Freundlich model suggests a more heterogeneous surface for the adsorbent [49]. In this experiment, the calculated value was 0.473, which was consistent with this concept. The calculated values for maximum capacity corresponding to Dubinin-Radushkevich, Radke-Prausnitz, UT, and Langmuir isotherms were 404, 600, 603, and 600 mg g\textsuperscript{-1}, respectively. It should be noted that the calculated values of UT and Radke-Prausnitz were equal and very close to the Langmuir model result. The values of the Dubinin-Radushkevich model was far below the experimental results.

![Fig. 4.](image)

![Fig. 5.](image)
3.6. Kinetic Studies

For determining and explaining the adsorption rate, it is vital to analyze kinetics data [43]. Various kinetics are used to examine the removal of CV by MRB at two different concentrations (500 and 750 mg L\(^{-1}\)). Residual root-mean-square error (RMSE), the result of kinetic parameters, the linear form of these kinetics, chi-square test \((\chi^2)\), and the coefficients of determination \((R^2)\) are shown in Table 3 [27, 51]. According to \((\chi^2)\), \(R^2\), and RMSE, liquid film diffusion and pseudo-first-order models were not successful in fitting experimental data, while the Elovich model showed a good fit for it. Also, it should be noted that the intra-particle diffusion model was better than the pseudo-second-order model. The experimental

<table>
<thead>
<tr>
<th>Model</th>
<th>Equation</th>
<th>Parameters</th>
<th>value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Dubinin-Radushkevich</td>
<td>(E = \frac{1}{\sqrt{2\beta}})</td>
<td>(E) : kJ mol(^{-1})</td>
<td>18.87</td>
</tr>
<tr>
<td></td>
<td>(\varepsilon = RT \ln \left(1 + \frac{1}{C_e}\right))</td>
<td>(\beta) : mol(^2) J(^{-2})</td>
<td>1.4\times10(^{-3})</td>
</tr>
<tr>
<td></td>
<td>(\ln q_e = \ln q_s - \beta \varepsilon^2)</td>
<td>(q_s) : mg g(^{-1})</td>
<td>404</td>
</tr>
<tr>
<td>UT Isotherm</td>
<td>(\ln \left(\frac{C_e - K_d}{C_m}\right) = -b \ln C_m + b \ln C_e)</td>
<td>(FCF)</td>
<td>0.314</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(b)</td>
<td>1.076</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(K_d) : mg L(^{-1})</td>
<td>113</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(q_m = \frac{C_m}{D}) : mg L(^{-1})</td>
<td>600</td>
</tr>
<tr>
<td>Langmuir</td>
<td>(\frac{C_m}{q_e} = \frac{1}{K_L q_m} + \frac{C_e}{q_m})</td>
<td>(K_L) : L mg(^{-1})</td>
<td>0.0093</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(q_m) : mg L(^{-1})</td>
<td>603</td>
</tr>
<tr>
<td></td>
<td>(R_L = \frac{1}{1 + K_L})</td>
<td>(R_L)</td>
<td>0.11-0.5</td>
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<tr>
<td>Radke-Prausnitz</td>
<td>(\frac{C_m}{q_e} = \frac{1}{K_{RP} q_m} + \frac{C_e}{q_m})</td>
<td>(K_{RP}) : L mg(^{-1})</td>
<td>5.62\times10(^{-3})</td>
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<tr>
<td></td>
<td></td>
<td>(q_m) : mg g(^{-1})</td>
<td>600</td>
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<td></td>
<td></td>
<td>(m)</td>
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<tr>
<td>Redlich-Peterson</td>
<td>(\ln \left(\frac{C_m}{q_e} \alpha_R\right) = g \ln C_e + \ln \alpha_R)</td>
<td>(\alpha_R) : (L mg(^{-1}))g</td>
<td>5.62\times10(^{-3})</td>
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<tr>
<td></td>
<td></td>
<td>(K_R) : L g(^{-1})</td>
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<td></td>
<td></td>
<td>(g)</td>
<td>1.076</td>
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<tr>
<td>Temkin</td>
<td>(q_e = B_1 \ln A + B_1 \ln C_e)</td>
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<td>129.1</td>
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<tr>
<td></td>
<td></td>
<td>(A) : L mg(^{-1})</td>
<td>0.096</td>
</tr>
<tr>
<td>Freundlich</td>
<td>(\ln q_e = \ln K_F + \frac{1}{n_F} \ln C_e)</td>
<td>(K_F) : (mg g(^{-3}))(L mg(^{-1}))(^{1/n})</td>
<td>29.31</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(1/n_F)</td>
<td>0.473</td>
</tr>
</tbody>
</table>

\(E\) : average energy of adsorption, \(\beta\) : Dubinin-Radushkevich constant, \(q_s\) : adsorption capacity, \(q_m\) : maximum capacity of adsorption, \(K_{RP}\) : constant of Radke-Prausnitz, \(FCF\) : UT dimensionless factor, \(b\) : UT exponent, \(K_d\) : desorption constant, \(K_F\) : Freundlich constant shows the adsorption capacity, \(1/n\) : Freundlich constant shows the adsorption intensity, \(\alpha_R\) and \(K_R\) : and \(g\) : constants of Redlich-Peterson, \(R\) : gas constant 8.314, \(K_L\) : Langmuir constant, \(B_1\) and \(A\) : constant of Temkin

Table 2. Parameters of Isotherm for CV Removal Using MRB
data and predicted data using kinetic models are indicated in Fig. S3. It is clear that Elovich and intra-particle diffusion models were well described all data.

At 298 K, by increasing concentration of dye (500 to 750 mg L\(^{-1}\)), the \(k_2\) (2.18 \times 10^{-4} to 9.69 \times 10^{-3} \text{ mg g}^{-1} \text{ min}^{-1}) decreased, so it can be concluded that adsorption is slower at lower concentration of CV.

The Fig. S1 (c) shows a schematic of the CV which is positively charged, attached to the negatively charged functional groups of adsorbent. Also, to identify the mechanism of adsorption, kinetics data were investigated by adsorption diffusion model. This model is based on three consecutive steps. The first step is diffusion across the liquid film surrounding the adsorbent particles (external diffusion or film diffusion). The second step is diffusion within the pores of adsorbent (internal diffusion or intra-particle diffusion). Finally the third step is adsorption of adsorbate by internal active sites [8]. The plot of \(\ln(1-(q_t/q_e))\) versus \(t\) should be a straight line if the film diffusion is the rate determining step. Also, the plot of \(q_t\) against \(t^{1/2}\) passing through the origin if the intra-particle diffusion act as the only rate-limiting step [47]. Otherwise, the adsorption kinetics may be controlled by film diffusion and intra-particle diffusion simultaneously. It was seen that in our experiment, the plotted line dose not pass through the origin, so both intraparticle diffusion and film diffusion are the rate-controlling step. Furthermore, the constant of intraparticle diffusion \((k_{id})\) increased by increasing dye concentration, as an outcome of the rise in the driving force.

Initial adsorption rate \((\alpha)\) and the desorption constant \((\beta)\) appear in the Elovich equation (Eq. (13)). High \(\beta\) value indicates a lower driving force [27]. According to Table 3, when CV concentration increases the Elovich constant \((\beta)\) decreases, and as a result, the adsorption constant \((\alpha)\) increases. This decrease in \(\beta\) is an indication of increasing the driving force (between CV and MRB molecules), and as a result better adsorption occurs.

### 3.7. Thermodynamic Study
To determine values of standard entropy \(\Delta S\) (J mol\(^{-1}\) K\(^{-1}\)), standard free energy \(\Delta G\) (J mol\(^{-1}\)) and standard enthalpy \(\Delta H\) (J mol\(^{-1}\)), the thermodynamic analysis was directed in CV removal by MRB at various temperature (279-328K) using following equations:

\[
K_s = \frac{q_e}{C_e}
\]  \hspace{1cm} (18)

\[
\Delta G = -RT \ln(K_s)
\]  \hspace{1cm} (19)
\[
\ln(K_e) = -\frac{\Delta H}{RT} + \frac{\Delta S}{R}
\]  

(20)

Where \( K_e \) is the distribution coefficient, \( T \) is the temperature (K), and \( R \) is the constant of thermodynamic gas (8.314 \( \text{J mol}^{-1} \text{K}^{-1} \)). The thermodynamic constants (\( \Delta G, \Delta S, \text{and } \Delta H \)) are given in Table S3 [51]. The adsorption of CV by MRB is an endothermic physisorption because the enthalpy (\( \Delta H \)) value was positive and less than 40 \( \text{J mol}^{-1} \text{K}^{-1} \) [35]. The \( \Delta S \) of adsorption had positive value since the randomness increased in the solid/solution interface. A negative amount of \( \Delta G \) displays CV removal using MRB is a spontaneous reaction.

3.8. Desorption Study

The adsorbent becomes more efficient if it can be reused. In that case, it would bring more economic and environmental benefits (46). To achieve this purpose, MRB was regenerated with a HCl solution (0.5 mol L\(^{-1}\)). After the adsorption process, MRB was separated from the CV solution, then it was mixed with HCl (0.5 mol L\(^{-1}\)) and shaken for 30 min. Subsequently, the resulting mixture was washed with deionized water. As Fig. S4 shows, five cycles of adsorption/desorption reduce the dye removal efficiency by 10%, which shows the excellent ability of regenerated MRB in CV removal.

3.9. Comparision of The Capacities of MRB with Other Materials for The CV Removal

Several adsorbents for the CV removal were used, which their maximum adsorption capacities are presented in Table S4. The adsorption capacity of MRB was much more than other agricultural waste materials; it can be concluded that modification of rice bran increased its adsorption capacity.

4. Conclusions

In this research, a simple technique was suggested for modification of rice bran, as advantageous utilization of agricultural waste, to remove CV from aqueous solutions. Rice bran was successfully modified. The removal efficiency was independent of pH in the range of 2-7. For optimization and modeling of the adsorption process, BBD of the RSM was used. ANOVA analysis indicated that utilized models in this study were appropriate. Increasing adsorbent dosage and contact time increased the CV removal. Different ions did not have an adverse influence on the dye removal owing to the strong tendency between the modified group of MRB and CV. Equilibrium and kinetic adsorption data were well fitted by Redlich-Peterson, UT and Radvke-Prausnitz isotherms and Elovich models, respectively. Kinetic models were studied at different concentrations. By increasing dye concentration, the Elovich constant (\( j_0 \)) and pseudo-second-order rate constant (\( k_2 \)) decreased. The most important properties of MRB include high adsorption capacity (603 mg g\(^{-1}\)) as well as the low cost and recoverability. The results of this study show that MRB has a high ability to eliminate CV from polluted effluents. Producing the adsorbent from MRB seems a proper replacement for conventional disposal methods.

Author Contributions

M.R. (Ph.D. student) conducted all experiments and data analyses and prepared the manuscript. M.B. (Ph.D., Associate professor) overseeing experiments and data analyses and revised the manuscript. N.M. (Ph.D., Professor) overseeing experiments and data analyses and revised the manuscript. M.A.A. (Ph.D., Professor) overseeing experiments and data analyses and revised the manuscript.

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